Count data collected using a robust design: models, results and recommendations

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MOTIVATION

We were motivated by data on butterflies collected at the MPG ranch. • MPG ranch

"Set in the heart of Montana's Bitterroot Valley, MPG Ranch lies on over 9,500 acres of rich undeveloped landscape. Established in 2009, MPG strives to preserve the natural communities that make this area beautiful and focuses on research to restore and protect native diversity."



DATA - ROBUST DESIGN

Sites at the ranch were visited and transects were walked *three times*, instead of once which is the case in the standard design (SD), during each visit.

Result: count data collected under the robust design (RD).^{1,2}



¹Pollock, K. H. (1982). A capture-recapture design robust to unequal probability of capture. The Journal of Wildlife Management 46, 752-757

⁴McCrea, R. S., & Morgan, B. J. T. (2014). Analysis of capture-recapture data. CRC Press: イミトイミト ミークへ C

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We are interested in

- estimating the number of butterflies at each site and
- modelling phenology³ at each site.

 $^{^{3}}$ Defined by the Oxford dictionary as "The study of cyclic and seasonal natural phenomena, especially in relation to climate and plant and animal life."

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Model

We extend the SD Matechou et al. $(2014)^4$ model to account for the RD.

The model is a Jolly-Seber^{5,6} type, motivated by more recent work in stopover capture-recapture models ^{7,8}, but does not require uniquely identifiable individuals.

⁵ Jolly, G. M. (1965). Explicit estimates from capture-recapture data with both death and immigration – Stochastic model. *Biometrika* 52, 225-247.

⁶Seber, G. A. F. (1965). A note on the multiple recapture census. *Biometrika* 52, 249-259.

⁷ Schwarz, C. J. and Arnason, A. N. (1996). A general methodology for the analysis of open-model capture recapture experiments. *Biometrics* **52**, 860-873.

⁸Pledger S., Efford M., Pollock K., Collazo J. A., Lyons, J. E. (2009). Stopover duration analysis with departure probability dependent on unknown time since arrival. In: DL Thompson, EG Cooch, MJ Conroy (eds) Modeling Demographic Processes in Marked Populations. Springer. pp. 349-363.

⁴ Matechou, E., Dennis, E. B., Freeman, S. N., Brereton, T. (2014). Modelling abundance and phenology in (multivoline) butterfly species: a novel mixture model. *JAE* **51**, 766-775

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Model

The model provides estimates of

- ► *N*: "super-population" size (site-specific)
- β: entry parameters. They describe the emergence pattern, which is modelled using the pdf of *G* normal distribution(s), where *G* is the number of broods of the species. Mean arrival time can be modelled as function of (site) covariates.
- ϕ : survival probability

while taking into account imperfect detection, i.e. *p* (which can vary according to site and time specific covariates).

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S = 20 sites were visited on T = 21 consecutive weeks and were each walked $K_t = 3$ times for t = 1, ..., T resulting in $20 \times 21 \times 3$ counts in total, although 702 counts (i.e. around 50%) are actually missing.

The species is univoltine so we set G = 1



The sites are located on different levels of elevation and hence we model the site mean emergence time of the species as a function of site elevation: $\mu_s = \alpha_0 + \alpha_1 x_s$ where x_s is the elevation of site *s*.

We model detection probability as a function of weather covariates

Model selection results for the small wood-nymph data collected in 2014. The models only differ in the constraints used for detection probability.

Model for <i>p</i>	ν	AIC
1. logit(p_{stk}) = γ_0	25	857.5
2. logit(p_{stk}) = $\gamma_0 + \gamma_1 z_{stk}$	26	860.5
3. logit(p_{stk}) = $\gamma_0 + \gamma_1 \mathbf{w}_{stk}$	26	850.5
4. logit(p_{stk}) = $\gamma_0 + \gamma_1 \mathbf{z}_{stk} + \gamma_2 \mathbf{w}_{stk}$	27	849.8

where z is temperature and w is % of cloudless sky.

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95% non-parametric bootstrap intervals obtained for N_1, \ldots, N_{20} left: our proposed RD model

right: the Matechou et al. (2014) model keeping one (out of three) counts at random.



95% non-parametric bootstrap intervals obtained for $\beta_0, \ldots, \beta_{19}$ left: site with lowest elevation right: site with highest elevation.

Estimated weekly survival: 0.52 (0.033, 0.696).

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CAN THE RD COMPENSATE FOR MISSING PRIMARY OCCASIONS?



MSE obtained for N for the SD(black) and the RD(gray) left: p only varies between primary occasions right: p also varies between secondary occasions.

WHAT IF THE MISSING PRIMARY OCCASIONS ARE MOSTLY AT THE START AND END OF THE SEASON?



MSE obtained for N for the SD(black) and the RD(gray) left: p only varies between primary occasions right: p also varies between secondary occasions.

DO WE NEED TO USE THE RD FOR ALL SITES?



MSE obtained for N for the SD(black) and the RD(gray) left: p only varies between primary occasions right: p also varies between secondary occasions.

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- The RD can improve accuracy of population size estimates. Other parameters are more robust to the sampling scheme used.
- This improvement can be substantial if detection probability depends on a covariate that varies between both primary and secondary occasions.
- The RD can be used to compensate for missing primary occasions. Example: fewer visits to the site but more counts obtained once there.
- ► This is especially true, with the RD performing better with fewer counts than the SD, if the covariate for *p* varies between both primary and secondary occasions and the missing counts are mostly concentrated at the start and end of season.

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More simulations! For example, answering questions such as: if one can only go to the site x% of the weeks, how many counts should they obtain once there to compensate?

Do you know of any schemes where several counts are obtained during each visit eg. double-observer schemes-or could easily be obtained but are not at the moment?

Thank you!

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